# Note

# EXCESS VOLUMES OF CYCLOALKANOL + *n*-ALKANE SYSTEMS IN TERMS OF AN ASSOCIATED SOLUTION THEORY WITH A FLORY EQUATION OF STATE CONTRIBUTION

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A model [1-5] for the excess volumes of binary systems comprising a self-associated component and an inert solvent was applied to some cycloalkanol + *n*-alkane systems. The estimated excess volumes correlate well with experimental results [6,7] for systems formed by mixing a cycloalkanol ( $C_5$ ,  $C_6$ ) with an *n*-alkane ( $C_6-C_8$ ,  $C_{10}$ ,  $C_{12}$ ).

## **RESULTS AND DISCUSSION**

In our model, the excess molar volume  $V^{E}$  is expressed as the sum of a chemical contribution described by an athermal associated solution of the Mecke-Kempter type, and a physical contribution obtained from the Flory equation of state. Details of the model and the relevant equations are given in our earlier publications [1-3]. The same notation is adopted here.

The characteristic values (pressure  $p^*$ , molar volume  $V^*$  and temperature  $T^*$ ) needed to evaluate the Flory equation of state contribution were calculated as previously [1,5,8] from the properties (molar volume  $V^\circ$ , isobaric thermal expansivity  $\alpha_p^\circ$ , and isothermal compressibility  $\kappa_T^\circ$ ) of the pure components, and are summarized in Table 1. A procedure, analogous to that used for pyridine base + *n*-alkane systems [3,4], was followed to establish the values of the four model parameters: the molar enthalpy  $\Delta h_{\rm H}^\circ$ , molar entropy  $\Delta s_{\rm H}^\circ$ , and molar volume  $\Delta v_{\rm H}^\circ$  of H-bond formation, and the Flory exchange interaction parameter  $X_{12}$ . The values  $\Delta h_{\rm H}^\circ = -24.4$  kJ mol<sup>-1</sup> and  $\Delta v_{\rm H}^\circ = -10$  cm<sup>3</sup> mol<sup>-1</sup> used previously for alkanols [1,2,5] were adopted in the present calculations.

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	$V^{\circ}$ (cm <sup>3</sup> mol <sup>-1</sup> )	α <sub>p</sub> <sup>ο</sup> (kK <sup>-1</sup> )	κ <sub>T</sub> (TPa <sup>-1</sup> )	p* (J cm <sup>-3</sup> )	$V^*$ (cm <sup>3</sup> mol <sup>-1</sup> )	T* (K)
Cyclopentanol [5]	91.342	0.829	620.0	585.2	75.392	5829
Cyclohexanol [5]	105.977	0.804	590.7	590.3	87.868	5939
n-Hexane [1]	131.597	1.387	1703.9	424.2	99.543	4436
n-Heptane [1]	147.448	1.256	1460.6	431.9	113.601	4648
n-Octane [1]	163.504	1.164	1302.4	436.8	127.698	4827
n-Decane [1]	195.945	1.051	11 <b>09.6</b>	447.0	155.750	5091
n-Dodecane [8]	228.550	0.960	987.7	445.2	184.397	5351

Molar volume  $V^{\circ}$ , isobaric thermal expansivity  $\alpha_p^{\circ}$ , and isothermal compressibility  $\kappa_T^{\circ}$  for the component liquids at 298.15 K, and characteristic values of the pressure  $p^*$ , molar volume  $V^*$ , and temperature  $T^*$  obtained from the Flory formalism

For a set of systems formed by the same cycloalkanol (component 1) with a series of n-alkanes (component 2), the relation

$$X_{12} = X_{12}^{\ddagger} \left( \frac{V_2^{\ast}}{V_2^{\ast \ddagger}} \right)^{\rho} \tag{1}$$

was assumed, where  $V_2^*$  is the characteristic molar volume for the *n*-alkane, and  $X_{12}^{\ddagger}$  and  $V_2^{*\ddagger}$  are the values of  $X_{12}$  and  $V_2^*$  for a reference system belonging to the set. In the present work, the system with *n*-hexane was used as the reference for each set, and the values of  $\Delta s_{\rm H}^{\circ}$  and  $X_{12}^{\ddagger}$  were determined to fit the experimental results for  $V^{\rm E}$  at cycloalkanol mole fractions  $x_1$  of 0.5 and 0.05.

Satisfactory correlations of the excess volumes of 1-alkanol + alkane [1,2] and cycloalkanol + cycloalkane [5] mixtures were based on using a value  $p = -\frac{3}{2}$  for the exponent in eqn. (1). However, preliminary calculations for the present systems indicated that  $X_{12}$  should increase more rapidly with increasing size of the *n*-alkane, and that a value  $p = -\frac{1}{2}$  was more appropriate. This behavioral difference from the previous alkanol + alkane systems may be due to the greater dissimilarity of the component molecules.

#### TABLE 2

Model parameters for cycloalkanol + *n*-alkane systems: exchange interaction coefficient  $X_{12}^{\ddagger}$  for the equation of state contribution; volume  $\Delta v_{H}^{\circ}$ , enthalpy  $\Delta h_{H}^{\circ}$ , and entropy  $\Delta s_{H}^{\circ}$  of self-association, and equilibrium constant K (T = 298.15 K) for the association contribution

Cycloalkanol	$X_{12}^{\ddagger}$ (J cm <sup>-3</sup> )	$\frac{\Delta v_{\rm H}^{\diamond}}{(\rm cm^3 \ mol^{-1})}$	$\frac{\Delta h_{\rm H}^{\circ}}{(\rm kJ\ mol^{-1})}$	$\frac{\Delta s_{\rm H}^{\circ}}{(\rm J~K^{-1}~mol^{-1})}$	K
Cyclopentanol	42.45	-10 <sup>a</sup>	-24.4 <sup>a</sup>	- 25.09	568.5
Cyclohexanol	49.52	- 10 ª	-24.4 ª	-24.83	503.3

<sup>a</sup> Adopted from previous work [1,2,5].

TABLE 1



Fig. 1. Excess molar volumes  $V^{E}$  for binary mixtures of cyclopentanol with some *n*-alkanes  $C_nH_{2n+2}$  at 298.15 K vs. mole fraction  $x_1$  of cyclopentanol. Curves: ——, smoothed experimental results [6,7]; — —, calculated from present theory. Curves are labelled with the value of *n*.

Thus, the formation of the present systems involves the mixing of molecules with cyclic and chain structures, and may lead to differences in the disruption of the cycloalkanol liquid structure (non-specific and H-bond interactions), as well as in packing effects and interstitial accommodation.

The values of the model parameters  $\Delta s_{H}^{\circ}$  and  $X_{12}^{\ddagger}$ , obtained from fitting the reference systems formed by each cycloalkanol with *n*-hexane, are given in Table 2. Also listed are the corresponding values of the classical equilibrium constant K for the association contribution at 298.15 K.

Excess molar volumes estimated for cycloalkanol + *n*-alkane systems, using the parameters obtained from the *n*-hexane reference system, are plotted in Figs. 1 and 2, where smoothed representations of the experimental results are shown for comparison. The model adequately expresses the concentration dependence of  $V^{\rm E}$  and its progressive change as the number of carbon atoms in the alkane chain is increased.



Fig. 2. Excess molar volumes  $V^{\rm E}$  for binary mixtures of cyclohexanol with some *n*-alkanes  $C_n H_{2n+2}$  at 298.15 K vs. mole fraction  $x_1$  of cyclohexanol. Curves: ——, smoothed experimental results [7]; — —, calculated from present theory. Curves are labelled with the value of *n*.

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#### REFERENCES

- 1 A.J. Treszczanowicz and G.C. Benson, Fluid Phase Equilibria, 23 (1985) 117.
- 2 A.J. Treszczanowicz and G.C. Benson, Fluid Phase Equilibria, 41 (1988) 31.
- 3 A.J. Treszczanowicz, D. Patterson, G.C. Benson and T. Kasprzycka-Guttman, Fluid Phase Equilibria, 50 (1989) 235.
- 4 A.J. Treszczanowicz, G.C. Benson and T. Kasprzycka-Guttman, Fluid Phase Equilibria, 62 (1991) 259.
- 5 A.J. Treszczanowicz and G.C. Benson, Thermochim. Acta, 179 (1991) 39.
- 6 A.J. Treszczanowicz and G.C. Benson, J. Chem. Thermodyn., 17 (1985) 123.
- 7 H. Kaur, J.R. Khurma and B.S. Mahl, Fluid Phase Equilibria, 45 (1989) 121.
- 8 G.C. Benson, C.J. Halpin and M.K. Kumaran, J. Chem. Thermodyn., 18 (1986) 1147.